

1.4 DATA TYPES & STRUCTURES · 1.4.3

Adders & D-type flip-flops

Logic that adds binary, and logic that remembers a bit. Spec 1.4.3(e).

01 Half adder

Adds Two bits A, B → sum S, carry C.

Sum $S = A \oplus B$ (XOR).

Carry $C = A \cdot B$ (AND).

Gates 1 XOR + 1 AND. No carry-in.

02 Full adder

Adds A, B and Cin → S, Cout.

Sum $S = A \oplus B \oplus \text{Cin}$

Cout $(A \cdot B) + (\text{Cin} \cdot (A \oplus B))$

Build Two half adders + OR; chain for multi-bit.

03 D-type flip-flop

Stores One bit of data.

Inputs D (data) and a clock.

Outputs Q and $\neg Q$.

How On the **clock edge**, Q takes the value of D, then **holds** it.

Use Building block of **registers & memory**; kept in step by the clock.

FINAL PASS BEFORE THE EXAM

Rapid exam tips

Six slips on adder/flip-flop questions.

01

Half-adder sum = **XOR** (not OR); carry = **AND**.

02

A **full** adder has a third input — the **carry-in**.

03

Full adder = **two half adders + OR**; chain them for multi-bit numbers.

04

Flip-flop inputs = **D + clock**; outputs = **Q and $\neg Q$** .

05

Q captures D on the **clock edge**, then **holds** until the next tick.

06

Adders **compute**; flip-flops **store**. Different jobs.