

2.3 ALGORITHMS · 2.3.1(C)(D)

Complexity & Big-O notation

How time/space grow with n , the Big-O classes & comparing algorithms. Spec 2.3.1(c)(d).

01 What complexity means

Time How steps grow with input n .

Space How memory grows with n .

Big-O **Worst-case** growth; drop constants, keep dominant term.

e.g. $3n + 5 \rightarrow O(n)$

02 Classes (best → worst)

$O(1)$ Constant — array index.

$O(\log n)$ Logarithmic — binary search.

$O(n)$ Linear — linear search.

$O(n^2)$ Polynomial — bubble/insertion sort.

$O(2^n)$ Exponential — brute-force subsets.

03 Spotting Big-O

1 loop $\approx O(n)$.

Nested loops $\approx O(n^2)$.

Halve each step $\approx O(\log n)$.

No loop $\approx O(1)$.

04 Comparing algorithms

Large n Lower growth wins: $\log n < n < n^2 < 2^n$.

Small n Constants matter — Big-O is about **scaling**.

Also Weigh **space** (e.g. merge sort needs extra memory).

FINAL PASS BEFORE THE EXAM

Rapid exam tips

Six slips on Big-O questions.

01

Drop constants: $2n+3 \rightarrow O(n)$. Keep the dominant term.

02

$O(n^2)$ = **polynomial**; $O(2^n)$ = **exponential**. Don't swap.

03

Single loop $\rightarrow O(n)$; **nested loops** $\rightarrow O(n^2)$.

04

Halving each step $\rightarrow O(\log n)$ (binary search).

05

Big-O = **large-n scalability**; small n, constants can matter.

06

bubble $O(n^2)$ vs merge $O(n \log n)$: merge scales far better.